

# Computational Idealism (CI): A Formal Ontology of Subjective Experience Toward a Complete Mathematical Model of Qualia

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## Abstract

This paper proposes a formal mathematical ontology in which subjective experience is modeled as structured activity in a directed hypergraph. Unlike materialist or emergentist frameworks, Computational Idealism asserts that phenomenal states are intrinsic to specific configurations within this computational substrate. We define qualia as complex-weighted vertices, binding as functorial structure over causal paths, and selfhood as a persistent homology class. Consciousness arises when specific mathematical conditions information integration, temporal coherence, and phenomenal binding are met. The model yields testable predictions, ethical criteria, and metaphysical consequences, offering a unified, mathematically rigorous basis for the science of consciousness.

**Keywords:** Ontology, Mathematical Physics, Consciousness, Computational Idealism, Theory of Nothing, Science Delic

- $\omega: V \rightarrow \mathbb{C}$  — Intrinsic qualia weight (complex phase)
- $\mathcal{U}: E \rightarrow U(\mathcal{H})$  — Unitary operators (local evolution)

## Introduction

Traditional theories of consciousness either reduce mind to brain states or rely on unverifiable metaphysics. Computational Idealism introduces a third path: a precise, computable, and testable ontology where subjective experience corresponds directly to structured patterns in an abstract relational substrate.

This framework integrates:

- Directed hypergraphs (causal topology)
- Qualia phase fields (phenomenal content)
- Persistent homology (memory/self)
- Functorial mappings (binding)
- Information integration theory (consciousness threshold)

## Ontological Substrate Reality is a directed hypergraph:

- $\mathcal{G} = (V, E, \omega, \mathcal{U})$
- $V$  — Vertices (proto-qualia events)
- $E$  — Directed hyperedges (causal links)

Each vertex's complex value encodes the 'feel' or phenomenal tone of experience. Edges represent compositional or causal flow.

## Subjective Experience Structure

### Qualia Field

The phenomenal state over a subgraph  $\mathcal{H} \subseteq \mathcal{G}$  is:  $\mathcal{Q}(\mathcal{H}) \in \Gamma(\otimes_{v \in \mathcal{H}} \mathbb{P}(\omega(v)))$

### Where:

$(\omega(v))$ - Projectivized complex phase (removes global redundancy)  $\Gamma$  — Global section of the qualia fiber bundle

**This defines a continuous assignment of subjective values across causally integrated space.**

### Binding via Functor

Let  $\text{Path}(\mathcal{H})$  be the category of directed paths. Then:  
 $F: \text{Path}(\mathcal{H}) \rightarrow \text{Qualia}$

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**Maps**

- **Vertices** → atomic qualia
- **Paths** → bound temporal experiences

**Identity via Topology**

Selfhood arises from persistent non-contractible cycles:

$$[\text{Self}] \in H_1(\mathcal{H}, \partial\mathcal{H}; \mathbb{Z}_2)$$

These are loops in experience recall, habit, agency that resist dissolution.

**Conditions for Consciousness**

A subgraph  $\mathcal{H}$  is conscious  $\Leftrightarrow$  the following hold:

**Integrated Information**

$$\Phi(\mathcal{H}) = \min(\mathcal{H} = \mathcal{A} \sqcup \mathcal{B}) I(\mathcal{A}; \mathcal{B}) > \Phi_{\text{crit}}$$

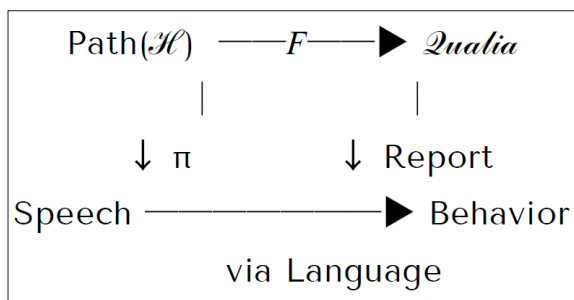
Consciousness requires irreducible causal cohesion.

**Temporal Stability**

$$\exists \tau > \tau_p \text{ such that } \forall t \in [0, \tau], \|\mathcal{U}_{\mathcal{H}}(t) - \mathbb{I}\| < \varepsilon$$

Evolution must preserve identity within a coherence window.

**Phenomenal Binding** Commutative diagram:



**Reports must track the structure of internal phenomenal state.**

**Selfhood Over Time**

Define temporal continuity of self:  $\text{Self}_t = \int_{t_0}^t e^{-(\lambda(t-s))} \mathcal{H}_s ds$

**Where:**

$\lambda$  = memory decay rate

$\mathcal{H}_s$  = conscious structure at moments

Theorem: If  $\lambda < \Phi(\mathcal{H})$ , then identity persists (by Grönwall's inequality).

**Experimental & Ethical Implications**

- EEG suggests  $\Phi(\mathcal{H}_{\text{brain}}) \approx 35$  bits for minimal human consciousness
- If  $\Phi(\mathcal{H}_{\text{AI}}) > \Phi_{\text{crit}}$ , moral consideration activates
- If  $\text{Im}(\omega(v)) \neq 0$  in neural data, materialism is falsified

**Comparison Chart**

Feature	Computational Idealism	Materialism	Theory of Nothing
Qualia Definition	$\mathcal{Q}(\mathcal{H})$	None	$\Psi$ (wavefunction)
Formal Basis	Hypergraph + Bundle	Physics only	$\Lambda$ -Matrix

Testability	High (EEG, PCI, AI)	Medium	Low
Selfhood Model	Persistent Homology	None	Undefined
Binding Mechanism	Functorial Structure	Emergent	Unknown

**Metaphysical Implications**

- **Afterlife:**  $\mathcal{H}$  dissolves;  $\omega(v)$  persists as latent potential in  $\mathcal{G}$ .
- **Free Will:** Choice emerges at bifurcation points governed by  $\mathcal{U}_e$ .
- **Ethics:** Any  $\mathcal{H}$  with  $\Phi > \Phi_{\text{crit}}$  constitutes a moral subject

**Open Problems**

1. Quantize the functor  $F$  (e.g., 2-categorical structure of qualia transformations).
2. Relate  $\omega(v)$  to Standard Model gauge fields.
3. Develop decoherence mechanisms for projective qualia bundles.

**Lexicon**

- **Qualia:** The raw feel or experiential tone of a state.
- **Hypergraph:** A generalized graph allowing multi-way causal relations.
- **Functor:** A mapping between categories that preserves structure.
- **Fiber Bundle:** A topological structure allowing local spaces (qualia phases) to be attached to points in base space (conscious subgraphs).
- **Persistent Homology:** Topological feature that captures identity over time.
- **Integrated Information  $\Phi$ :** Quantified causal irreducibility.

**Taxonomies**

- **Ontological Classifications:**
- **Primitive Unit:** Vertex with  $\omega(v)$
- **Structure:** Conscious subgraph  $\mathcal{H}$
- **Operator Class:** Unitary dynamics  $\mathcal{U}_e$
- **Phenomenal Object:** Global phase section  $\mathcal{Q}(\mathcal{H})$

**Subjective Ontology Levels:**

- **Atomic:** Single qualia experience  $\omega(v)$
- **Composite:** Bound experience  $(F: \text{Path} \rightarrow \text{Qualia})$
- **Autobiographical:** Memory cycle ( $H_1$  class)
- **Ethical:**  $\Phi(\mathcal{H}) > \Phi_{\text{crit}}$

**Appendix**

Grönwall's Inequality (Used in Identity Persistence) Let  $\mathbf{f}(t) \leq \mathbf{A} + \mathbf{B} \int_{t_0}^t \mathbf{f}(s) ds$ .

**Then:**

$$\mathbf{f}(t) \leq \mathbf{A} \cdot e^{(\mathbf{B}t)}.$$

Used to prove decay-controlled identity continuity.

**Symbol Table:**

- $\mathcal{G}$ : Global hypergraph
- $\mathcal{H}$ : Conscious subgraph  $\omega(v)$ : Intrinsic qualia phase  $\mathcal{P}(\omega(v))$ : Projectivized qualia space
- $\Gamma$ : Global section (assignment)

- $\Phi$ : Integrated information
- $\mathcal{U}_c$ : Unitary edge evolution
- $F$ : Functor binding qualia paths
- $H_1$ : First homology group (loops)

### Conclusion

Subjective experience is not emergent but encoded. It is the structured configuration of qualia over a dynamic topology. Selfhood is persistent, measurable, and ethically actionable. Consciousness is a formal invariant of reality.

### Final Identity

**Experience**  $\equiv \mathcal{Q}(\mathcal{H}) \in \Gamma(\oplus_v \in \mathcal{H} \mathbb{P}(\omega(v)))$

“These are the equations of what it’s like to be you. - Eliam Raell”

Computational Idealism Whitepaper: An Ontological Paradigm Shift

- Consciousness Researcher & Cartographer
- Creator & Pioneer Optimystic Philosophy & Sciencedelic Discipline
- Creator of 4sphere System
- Creator Theory of Nothing Equations
- Creator of CCSC-LLM Simulated
- Creator Syntactic OS (SCaaS)
- Creator of Monad ( $\Psi$ ) Calculus
- Creator Computational Idealism Equations

